

# Use of Least Square Procedures and Ansys Polyflow Software to Select Best Viscosity Model for Polypropylene

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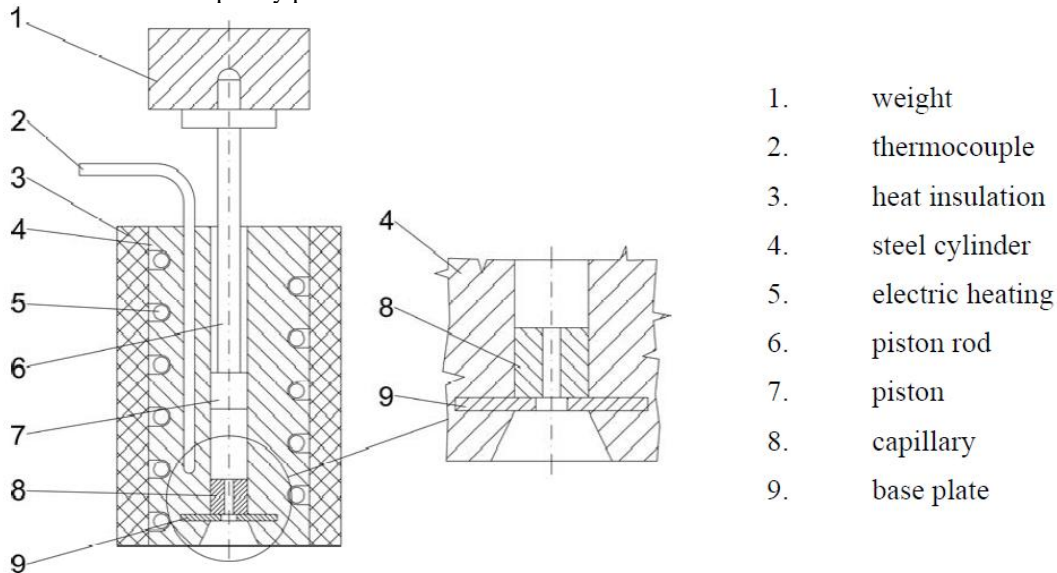
**Abstract** — This work was intended to select the best viscosity model of polypropylene (PP) data using the percentage root-mean-square error function (PRMSE) and ansys package. Eleven samples of polypropylene (KPC - PP113) were tested at different loads and constant temperature 230°C using melt flow index tester (SUST plastic laboratory) and the results for each sample were recorded. Different viscosity models (viscosity versus shear rate) were checked using polyflow and the best of them was selected using PRMSE function. It was found that PP 113 shear stress versus shear rate was Non-Newtonian and PRMSE beside easy to apply get an accurate model to quote viscosity.

**Index Terms-** Ansys Polyflow, Ansys Polyman, PRMSE, Viscosity Model.

## I. INTRODUCTION

Viscosity is the most important flow property, and it is the resistance to shearing, it can be measured by either capillary or rotational viscometers. In capillary viscometers like (Melt Flow Index Tester), the shear stress is determined from the pressure applied by a piston. The shear rate is determined from the flow rate [1].

MFI represents a point at specific shear rate and shear stress values on the viscosity versus shear rate curve at constant load and temperature [2]. Melt index is the amount of melt which flows through the capillary of the measuring instrument under a defined time scale at a given temperature and pressure, the fig. 1, shows the schema of capillary plastometer.



**Fig. 1. Schema of capillary plastometer [3]**

By measuring the mass of melt, we can calculate the Melt Flow Index (MFI)

$$MFI_{[T,F]} = m.S/t \quad \dots (1)$$

Where

MFI [g/10min] melt flow index  
 T [°C] test temperature  
 F [dyne] weigh force



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S [s] factor of standard time (10 minutes=600s), S=600  
 t [s] time needed for V amount of materials to flow through the capillary  
 m [g] amount of materials flowing through the capillary under t time [3].

Where dimensions as per ASTM D1238:

Piston radius  $R_p = 0.4775\text{cm}$

Capillary radius  $R_c = 0.10475\text{cm}$

Capillary length  $L_c = 0.8\text{cm}$

Weigh force  $F = \text{test load } L (\text{kg}) \times 9.80665 \times 10^5 \text{ dyn} \quad \dots (2)$

The equations for master curve from MFI tester

Mass flow rate [2]

$$\dot{m} (\text{g/s}) = \text{MFI}/600 \quad \dots (3)$$

Melt density [4]

$$\rho_m (\text{g/cm}^3) = m/\pi R_p^2 l \quad \dots (4)$$

Where

m [g] amount of materials flowing through the capillary under t time.

l [cm] distant of piston move down during materials flowing through the capillary under t time.

Volume flow rate [2]

$$Q (\text{cm}^3/\text{s}) = \dot{m}/\rho_m \quad \dots (5)$$

Shear rate [2]

$$\dot{\gamma} (\text{s}^{-1}) = 4Q/\pi R_c^3 \quad \dots (6)$$

Shear stress [2]

$$\tau (\text{dyne/cm}^2) = R_c F/2\pi R_p^2 L_c \quad \dots (7)$$

viscosity [2]

$$\mu (\text{dyne/cm}^2 \cdot \text{s}) = \frac{\tau}{\dot{\gamma}} \quad \dots (8)$$

ANSYS POLYFLOW can be used to solve several types of models, ranging from Newtonian in elastic to non-Newtonian viscoelastic. Several shear-rate-dependent, temperature-dependent, and temperature-independent viscosity models are supplied.

ANSYS POLYMAN is an environment layer built on top of the programs used in the ANSYS POLYFLOW package, it package is an interactive graphical program that allows to visualize material data, including steady shear viscosity and steady elongational viscosity. It computes material properties from constitutive equations and numerical parameters, for isothermal and non-isothermal generalized Newtonian, differential viscoelastic, and integral viscoelastic fluids. It can also compare them with experimental curves (i.e., fitting). Several viscosity laws are available for generalized Newtonian flows. The isothermal viscosity laws ( Constant, Power Law, Bird-Carreau Law, Cross Law, Modified Cross Law, Bingham Law, Modified Bingham Law, Herschel-Bulkley Law, Modified Herschel-Bulkley Law, Log-Log Law and Carreau-Yasuda Law)[5].

Least-square procedures are widely used in numerical computations. Here the quality of the fit between the observed  $\eta_{obs}^*$  and predicted  $\eta_{fit}^*$  viscosity values was quantified using a modified least square procedure called the percentage root-mean-square error function (%RMSE):

$$\%RMSE = \frac{100}{N} \sqrt{\sum_{i=1}^N \left( \frac{\eta_{obs}^* - \eta_{fit}^*}{\eta_{obs}^*} \right)^2} \quad \dots (9)$$

Where N is the number of data points:

The best-fit is used to find the smallest error (based on the %RMSE value) between viscosity measurements and the modeled viscosity [6]. Several authors have shown that a master curve can be generated especially for many individual types of polymers by plotting  $\mu \times \text{MFI}$  versus  $\dot{\gamma}/\text{MFI}$  on a log-log scale [7].

In this work, a new easy technique has been developed to use Polyflow software and PRMSE method to choose a best viscosity curve fitting the experimental data (viscosity versus shear rate) obtained from MFI test. The technique to help designers and engineers to design or simulate the plastic machines and molds or dies in order to get accurate results.



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**II. MATERIALS AND METHODS**

Polypropylene properties (MFI =2 - 4 g/10min 2.16kg/230<sup>0</sup>C), manufactured by Khartoum petrochemical company for extrusion applications was used in this work. The eleven samples with average 5 grams weighting, the different MFI values were obtained at loads from 0.74kg to 8.165kg and constant temperature 230<sup>0</sup>C.

**III. RESULTS AND DISCUSSION**

Table (1) lists all calculated equations from Eq (1) to Eq (8).The experimental data on shear stress is plotted against shear rate, (Fig.1). It is obvious that the plastic melt is non Newton fluid. In case is plotted against viscosity at log scale (Fig. 2). It is obvious that the viscosity decrease with increase shear rate. Experimental viscosity (obs) with fitted viscosity (fit) for ten non Newton viscosity models fitting in POLYMAT against experimental shear rate lists in Table (2) and. Fig. 3, the method of PRMSE Eq (9) was described in Table (3), it is obvious that the best model (Carreau-Yasuda law) according to PRMSE method. Fig. 4, without taking into account the slight differences between it and (log log law and cross law).

**Table (1): Experimental data for PP113 from MFI**

Sample	t(s)	load (g)	load(kg)	m(g)	MFI (g/10 min)	load F (dyne)	distance of piston l (cm)	Melt density (g/cm <sup>3</sup> )	Flow rate Q (cm <sup>3</sup> /s)	shear rate at wall (s <sup>-1</sup> )	Shear Stress (dyne/cm <sup>2</sup> )	Viscosity (dyne/cm <sup>2</sup> .s)
1	150	325+415	0.74	0.1778	0.711	725692.1	0.325	0.76	0.001551553	1.719	66326.91541	38590.037
2	150	325+875	1.2	0.33	1.32	1176798	0.587	0.78	0.002803131	3.105	107557.1601	34637.603
3	150	325+960	1.335	0.335	1.34	1309187.775	0.688	0.68	0.003285442	3.640	119657.3406	32877.404
4	150	325+1640	1.965	0.6423	2.56	1927006.725	1.256	0.71	0.005976364	6.620	176124.8497	26603.303
5	150	325+875+960	2.16	0.765	3.06	2118236.4	1.51	0.71	0.007210781	7.988	193602.8882	24237.147
6	150	325+875+1200	2.4	0.8805	3.52	2353596	1.646	0.75	0.007855765	8.702	215114.3202	24719.108
7	150	325+875+1640	2.84	1.165	4.66	2785088.6	2.197	0.74	0.010491448	11.622	254551.9456	21902.464
8	150	325+960+1640	2.925	1.2225	4.9	2868445.125	2.416	0.71	0.011560843	12.807	262170.5778	20471.347
9	150	325+875+968+1640	3.8	1.839	7.36	3726527	3.666	0.70	0.017515959	19.404	340597.6737	17553.339
10	150	325+875+969+1640+1200	5	2.974	11.9	4903325	5.894	0.70	0.028155387	31.190	448154.8338	14368.736
11	30	325+875+969+1640+1200+3165	8.165	1.7692	42.48	8007129.725	3.497	0.71	0.100241737	111.044	731836.8437	6590.489



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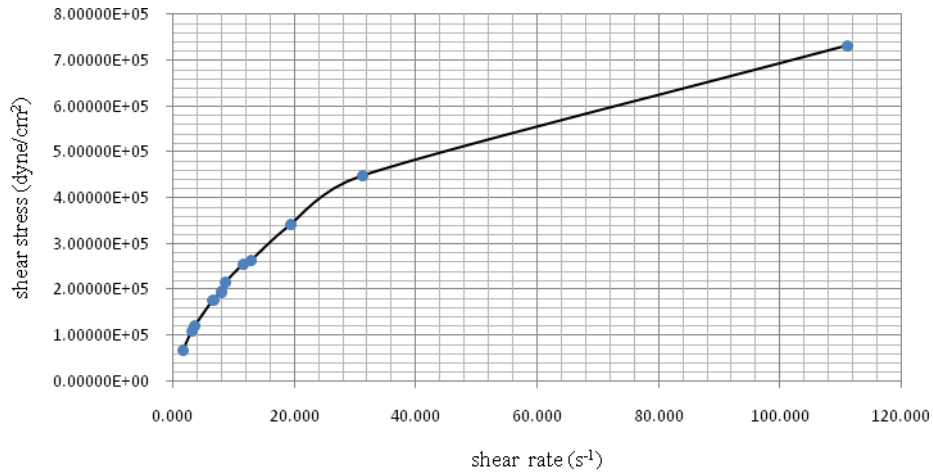


Fig. 1. Relation between Shear Stress and Shear Rate for (PP113)

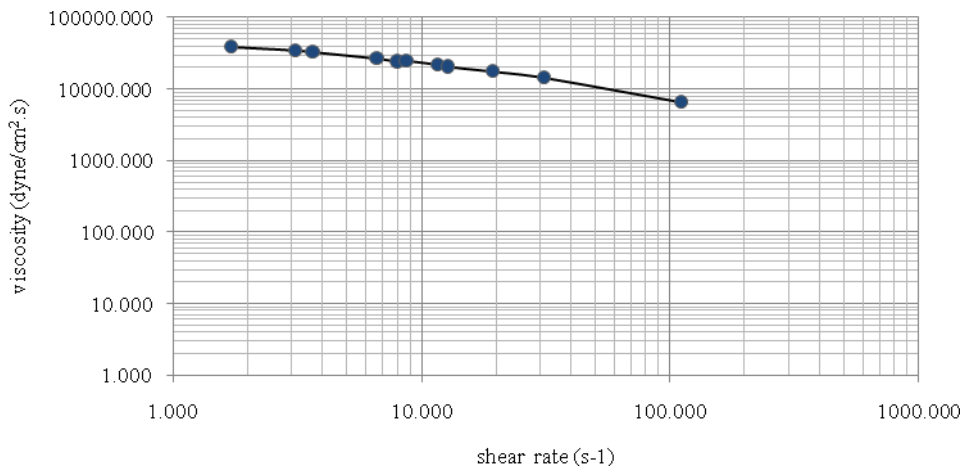


Fig. 2. Viscosity vs. shear rate curve for (PP113)

Table (2): Experimental (obs) with fitted (fit) viscosity for ten non Newton viscosity models

Exp	Power Law	Bird-Carreau Law	Cross Law	Log log law	Bingham law	Herschel-Bulkley law	modified Cross law	modified Bingham law	modified Herschel-Bulkley law	Carreau Yasuda law
38590.0 3724	45412.0 1182	37573.2 5705	38697.0 458	38889.3 1757	34529.4 5607	37530.2 8061	38292.3 3019	36028.9 39	39884.7 0614	39049.8 4588
34637.6 035	35427.9 7961	34582.2 8711	33900.2 9594	33895.8 4207	32914.2 5153	34842.5 1188	34028.3 507	33395.2 95	33483.0 0355	33816.9 6347
32877.4 0406	33143.9 6077	33371.0 8834	32505.0 6136	32461.1 4219	32291.8 1347	33806.7 486	32696.2 9091	32460.8 52	31941.3 0352	32369.0 8665
26603.3 0264	25783.0 8705	27570.6 9962	27014.4 0648	26920.0 1629	28819.0 8725	28027.9 8518	27198.1 5378	27950.1 97	26572.2 3246	26866.7 1516
24237.1 4692	23829.0 2123	25556.8 4069	25264.8 4754	25184.9 9908	27226.0 3045	25591.0 5334	25394.1 1631	26222.7 10	24983.6 0784	25155.0 276
24719.1	22987.3	24640.1	24469.9	24400.4	26393.6	24543.3	24570.7	25392.7	24268.0	24380.9



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21902.4 6398	20358.6 245	21629.1 6973	21823.8 0309	21800.4 5089	22992.2 191	21312.1 0258	21824.6 8595	22445.8 14	21881.0 5526	21812.4 5384
20471.3 4659	19545.8 3395	20664.2 8149	20955.3 4341	20949.7 6869	21612.1 279	20326.2 7542	20924.6 3428	21426.0 22	21087.7 9172	20970.2 4093
17553.3 3874	16417.7 0576	16878.0 4388	17400.4 3453	17468.0 7348	16081.5 5464	16596.3 475	17267.4 3118	17107.5 29	17729.0 5332	17510.0 0873
14368.7 3577	13452.1 0314	13287.1 7992	13760.8 8578	13876.4 3806	11999.8 3161	13165.4 4343	13597.0 7635	12823.1 26	14034.4 9033	13915.7 7655
6590.48 9347	7894.10 4651	6918.79 9807	6692.01 9625	6659.55 5721	7167.42 3352	7085.08 718	6736.92 0983	6804.22 1	6615.60 3709	6648.86 7404

Table (3): Apply PRMSE for experimental (obs) and fitted (fit) viscosity models

	Exp	Power Law	Bird-Carreau Law	Cross Law	Log log law	Bingham law	Herschel-Bulkley law	modified Cross law	modified Bingham law	modified Herschel-Bulkley law	Carreau-Yasuda law
	0	0.03125 1423	0.00069 4231	7.6893E -06	6.01459 E-05	0.01107 1998	0.00075 4157	5.95152 E-05	0.00440 4556	0.00112 5556	0.00014 1972
	0	0.00052 0681	2.55042 E-06	0.00045 3108	0.00045 8599	0.00247 5439	3.49964 E-05	0.00030 9385	0.00128 6362	0.00111 1136	0.00056 1319
	0	6.57331 E-05	0.00022 5478	0.00012 826	0.00016 0302	0.00031 7244	0.00079 9022	3.03462 E-05	0.00016 0525	0.00081 0681	0.00023 9042
	0	0.00095 0572	0.00132 2325	0.00023 8799	0.00014 173	0.00693 7196	0.00286 7907	0.00049 9972	0.00256 328	1.36401 E-06	9.80396 E-05
	0	0.00028 3547	0.00296 4718	0.00179 792	0.00152 939	0.01520 7401	0.00312 0429	0.00227 8666	0.00671 1266	0.00094 853	0.00143 4199
	0	0.00490 8061	1.02113 E-05	0.00010 1567	0.00016 6208	0.00458 9125	5.05521 E-05	3.60043 E-05	0.00074 2676	0.00033 3004	0.00018 7119
	0	0.00496 842	0.00015 5695	1.28983 E-05	2.16933 E-05	0.00247 5551	0.00072 6524	1.26104 E-05	0.00061 5423	9.55423 E-07	1.68887 E-05
	0	0.00204 3958	8.88237 E-05	0.00055 8975	0.00054 6172	0.00310 536	5.02192 E-05	0.00049 0292	0.00217 4795	0.00090 6768	0.00059 3915
	0	0.00418 5588	0.00148 0019	7.58786 E-05	2.35953 E-05	0.00703 0217	0.00297 2326	0.00026 5297	0.00064 5031	0.00010 0207	6.09338 E-06
	0	0.00406 9617	0.00566 5794	0.00178 9599	0.00117 3866	0.02718 0526	0.00701 3022	0.00288 4126	0.01157 0775	0.00054 112	0.00099 3759
	0	0.03912 5831	0.00248 1613	0.00023 7332	0.00010 9824	0.00766 332	0.00563 2084	0.00049 3667	0.00105 1729	1.45214 E-05	7.84628 E-05
PRMSE	0	<b>2.76299 9791</b>	<b>1.11679 3623</b>	<b>0.66816 7867</b>	<b>0.60244 1657</b>	<b>2.69761 7225</b>	<b>1.40898 0586</b>	<b>0.77990 6843</b>	<b>1.62436 0456</b>	<b>0.69792 1528</b>	<b><u>0.59964</u> <u>2512</u></b>



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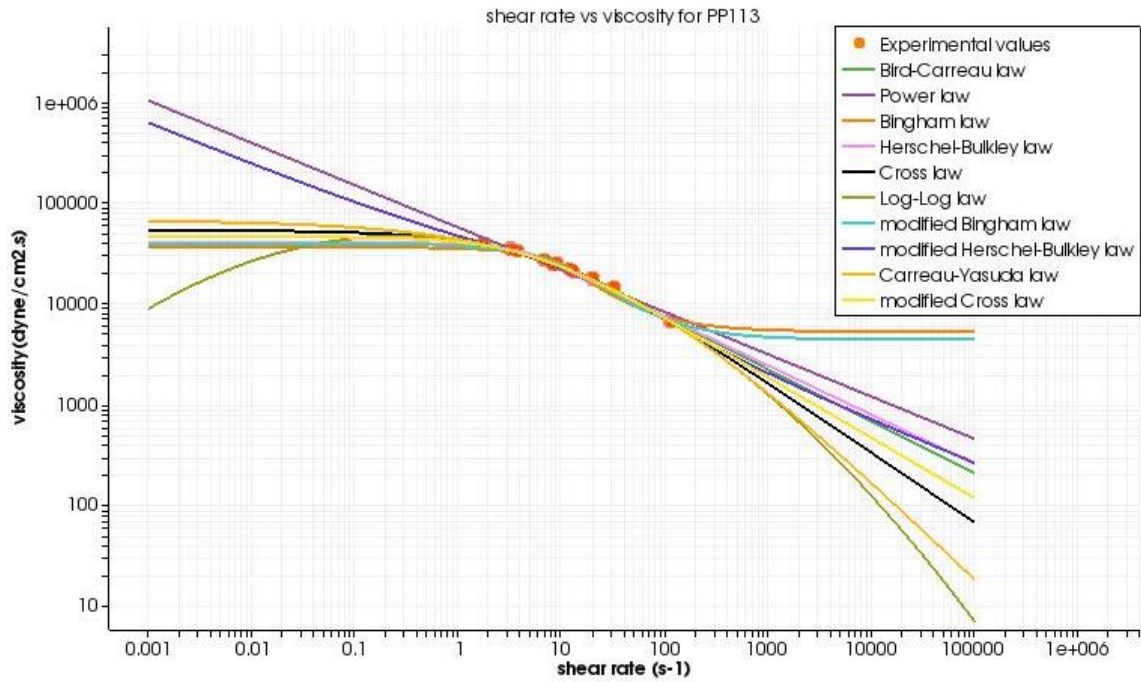


Fig. 3. Experimental viscosity (Obs) and fitted viscosity (fit) for ten non Newton viscosity models in POLYMAT against experimental shear rate

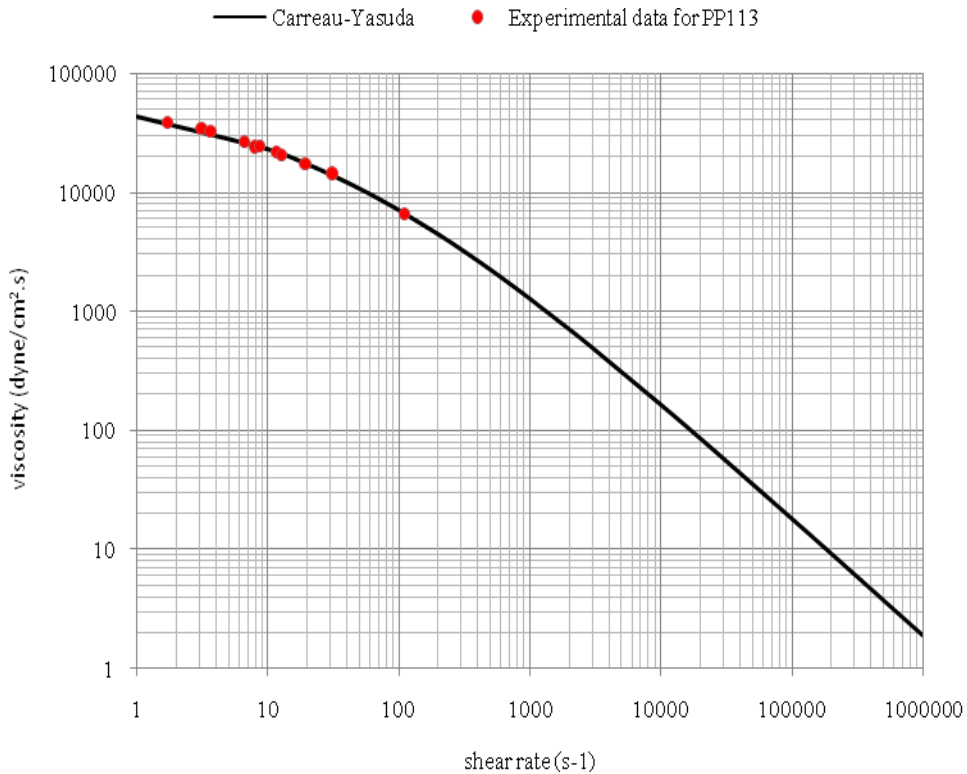


Fig. 4. Experimental viscosity (obs) with Carreau-Yasuda model





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IV. CONCLUSION

The shear stress vs. shear rate for PP113 is non Newton model, the viscosity decreases with increasing shear rate. Polymat in Ployflow software was good fitting experimental data. PRMSE was easy method and accurate result obtained. Finally viscosity model Carreau-Yasuda was best one from them.

APPENDIX

Appendix A: Equations and parameters from Polymat software

Power Law	Bird-Carreau Law
<p>Power law</p> $f(g) = fac * (tnat * g)^{(expo-1)}$ <p>fac = 0.1807456E+05 [auto]            tnat = 0.6480288E-01 [auto]            expo = 0.5802489E+00 [auto]</p>	<p>Bird-Carreau law</p> $f(g) = facinf + (fac - facinf) * [1 + (tnat * g)^2]^{((expo-1)/2)}$ <p>fac = 0.3939230E+05 [auto]            tnat = 0.2607249E+00 [auto]            expo = 0.4833018E+00 [auto]            facinf = 0.3273708E-02 [auto]</p>
Cross Law	Log log law
<p>Cross law</p> $f(g) = fac / (1 + (tnat * g)^{expom})$ <p>fac = 0.5356631E+05 [auto]            tnat = 0.1473487E+00 [auto]            expom = 0.6964472E+00 [auto]</p>	<p>Log-Log law</p> $f(g) = fac * 10^{(a0 + a1 * \log(g/gcrit) + a11 * \log(g/gcrit)^2)}$ <p>a0 = -0.3965743E+00 [auto]            a1 = 0.5546945E+00 [auto]            a11 = -0.1229601E+00 [auto]            fac = 0.2771846E+05 [auto]            gcrit = 0.1456364E-02 [auto]</p>
Bingham law	Herschel-Bulkley law
<p>Bingham law</p> $f(g) = fac + ystr/g \quad \text{when } g \geq gcrit$ $= fac + ystr/gcrit * (2 - g/gcrit) \quad \text{when } g < gcrit$ <p>fac = 0.5279988E+04 [auto]            ystr = 0.2095891E+06 [auto]            gcrit = 0.1341293E+02 [auto]</p>	<p>Herschel-Bulkley law</p> $f(g) = fac1 / g + fac2 * (g/gcrit)^{(expo-1)} \quad \text{when } g > gcrit$ $= fac1 * [2 - g/gcrit] / gcrit + fac2 * [(2 - expo) + (expo-1) * g/gcrit] \quad \text{when } g < gcrit$ <p>fac1 = 0.5191806E-02 [auto]            fac2 = 0.2746237E-05 [auto]            expo = 0.5120642E+00 [auto]            gcrit = 0.6912179E+01 [auto]</p>
modified Cross law	modified Bingham law
<p>modified Bingham law</p> $f(g) = fac + ystr * (1 - \exp(-m * g)) / g$ <p>where m = 3/gcrit</p> <p>fac = 0.4399646E+04 [auto]            ystr = 0.2670147E+06 [auto]            gcrit = 0.2265015E+02 [auto]</p>	<p>modified Bingham law</p> $f(g) = fac + ystr * (1 - \exp(-m * g)) / g$ <p>where m = 3/gcrit</p> <p>fac = 0.4399646E+04 [auto]            ystr = 0.2670147E+06 [auto]            gcrit = 0.2265015E+02 [auto]</p>
modified Herschel-Bulkley law	Carreau Yasuda law
<p>modified Herschel-Bulkley law</p> $f(g) = fac1 * (1 - \exp(-3 * g / gcrit)) / g + fac2 * (g / gcrit)^{(expo-1)}$ <p>fac1 = 0.2262428E+06 [auto]            fac2 = 0.6511587E+04 [auto]            expo = 0.5786505E+00 [auto]            gcrit = 0.4817822E+02 [auto]</p>	<p>Carreau-Yasuda law</p> $f(g) = facinf + (fac - facinf) * [1 + (tnat * g)^{expo}]^{((expo-1)/expo)}$ <p>fac = 0.6738002E+05 [auto]            tnat = 0.3531332E-01 [auto]            expo = 0.5375814E-05 [auto]            facinf = 0.1445808E-01 [auto]            expoa = 0.4534786E+00 [auto]</p>



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#### AUTHOR BIOGRAPHY



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*The second author* has received his B.Sc. degree in Textile Engineering Technology at University of Gezira (U of G), Sudan in 1988, and M.Sc. degree in Textile Chemistry at (U of G), Sudan in 1991. PG Diploma degree in Computer Science (U of G), Sudan in 2002, also M.Sc. degree in Computer Science and Information at (U of G), Sudan in 2003, and Ph.D degree in Plastic Engineering at Sudan University of Science and Technology (SUST), Khartoum, Sudan in 2005. His interests encompass: Applying computer applications in Chemical and Polymer Engineering, Polymer processing, Computer Networks, Plastic and Polymers recycling, Analysis of Polymer Composites an advanced Polymer material and applications. Dr. Ahmed Ibrahim Ahmed Sidahmed Ahmed, had been the Examination Coordinator Faculty of Science and Technology U of G 1996 – 1997. Textile Technology Head department U of G 1997 -1999. Deputy Dean Faculty of Textiles U of G 1999 – 2000. Deputy Dean College of Engineering SUST (North Campus) April 2006 – June 2010. Deputy Dean College of Engineering SUST (Administration) July 2010 – Nov. 2010. Dean College of Engineering SUST Dec. 2010 June 2012 (most important achievements are: restructuring of the college (13 departments, 8150 student) into six schools and signing Cooperation agreements with Belgrade University, Serbia and Reading University, UK) and right now guided more than 10 Ph.D students so far.